doi:10.3846/16111699.2012.670134

# INFLATION, INFLATION UNCERTAINTY AND GROWTH IN THE IRANIAN ECONOMY: AN APPLICATION OF BGARCH-M MODEL WITH BEKK APPROACH

## Hassan Heidari<sup>1</sup>, Salih Turan Katircioglu<sup>2</sup>, Sahar Bashiri<sup>3</sup>

<sup>1,3</sup>Department of Economics, Urmia University, Urmia, 165 Iran
<sup>2</sup>Department of Banking and Finance, Eastern Mediterranean University,
Famagusta, North Cyprus, Mersin 10, 95 Turkey
E-mails: <sup>1</sup>h.heidari@urmia.ac.ir; <sup>2</sup>salihk@emu.edu.tr (corresponding author);
<sup>3</sup>sahar.bashiri01@vahoo.com

Received 12 October 2011; accepted 23 February 2012

Abstract. This paper investigates the relationship between inflation, economic growth and their respective uncertainties in Iran for the period of 1988–2008 by using quarterly data. We employ a Bivariate Generalized Autoregressive Conditional Heteroskedasticity-in-Mean (BGARCH-M) model to examine in a unified empirical framework all the possible interactions between inflation uncertainty and growth in Iran. The model is simultaneously estimated by using the maximum log-likelihood method with the BEKK approach. The main findings of the present study are: (1) Inflation causes inflation uncertainty, supporting the Friedman-Ball hypothesis. (2) Inflation uncertainty affects the level of economic growth, supporting the Friedman (1977) hypothesis. (3) Growth uncertainty does not affect the level of economic growth, supporting the Friedman (1968) hypothesis. (4) And finally our empirical evidence shows that growth uncertainty affects the level of inflation, supporting the Deveraux (1989) hypothesis.

**Keywords:** inflation uncertainty, growth uncertainty, BGARCH-M, BEKK approach, Iran.

**Reference** to this paper should be made as follows: Heidari, H.; Katircioglu, S. T.; Bashiri, S. 2013. Inflation, inflation uncertainty and growth in the Iranian economy: an application of BGARCH-M model with BEKK approach, *Journal of Business Economics and Management* 14(5): 819–832.

JEL Classification: C22, E0.

#### 1. Introduction

In the last two decades, there has been an increasing interest in empirical research relating to economic growth in the case of Iran. In recent years a few papers constructed a large set of possible explanatory variables and employed econometric techniques to identify the variables which have a statistically significant impact on economic growth of Iran (Moshiri, Jahangard 2004; Mohammadi, Akbari Fard 2008; Komijani, Nazari 2009). However, studying the impact of inflation uncertainties on real income growth in the close economy of Iran deserves attention from researchers.

Heidari and Yengjeh (2010), Heidari *et al.* (2010), and Heidari and Bashiri (2011) consider uncertainty in their studies with the Iranian data. In these studies, they all employ Generalized Autoregressive Conditional Heteroskedasticity (GARCH) models and proxied inflation and output uncertainty by the conditional variance of shocks to inflation and output growth, respectively. GARCH models have been extensively employed in the studies for stock markets as well (Teresiene 2009). Results of Heidari and Yengjeh (2010) suggest no significant relationship between inflation uncertainty and real growth. Moreover, results of Heidari *et al.* (2010) reveal that growth uncertainty does not affect the level of economic growth, while Heidari and Bashiri (2011) show that growth uncertainty affects the level of inflation. The most important drawback of these studies is that, they have used a univariate GARCH specification for estimation of more than one series. There is a vast theoretical literature that emphasizes the importance of simultaneous effects of inflation and growth uncertainty on economic growth (Friedman 1968; Friedman 1977; Black 1987; Deveraux 1989; Holland 1993).

There is a lot of empirical evidence in the literature, which address this issue by applying bivariate models. For example, Grier et al. (2004) and Shields et al. (2005), by using a Bivariate GARCH (BGARCH) model, find that inflation uncertainty decreased inflation and output growth for the US, but output uncertainty increased growth but reduced inflation. Karanasos and Kim (2005) employ a BGARCH model of inflation and output growth to investigate the relationship between nominal and real uncertainty in the G3. They find that for the entire sample period 1957–2000, in all three countries, there is no causal relationship between nominal and real uncertainty. Moreover, they find different results (causal direction) for these three countries in different sub-samples. Narayan et al. (2009) use the EGARCH model to examine the relationship among output, inflation and their respective uncertainties for China. Their results suggest that Chinese output-inflation behaviour is consistent with the hypothesis that increased inflation uncertainty lowers average inflation; the hypothesis that inflation volatility reduces economic growth and the hypothesis that higher output volatility increases economic growth. They also find no support for the Deveraux (1989) hypothesis that output uncertainty has a positive impact on the level of inflation. Bhar and Mallik (2010) show that inflation uncertainty has positive and significant effect on the level of inflation and a negative and significant effect on the output growth. Their results, however, reveal that output uncertainty has no significant effect on output growth or inflation. Conrad et al. (2010) by using a BGARCH model find that inflation has a positive impact on both inflation and growth uncertainties. Their results also show that not only uncertainty of inflation and growth affect the level of inflation and growth but the level of inflation and growth affect their respective uncertainties.

To the best of our knowledge, there isn't any empirical study on assessing the relationship between inflation, economic growth and their respective uncertainties in the case of the Iranian data. However, this relationship with other countries' data has been mixed (Grier, Perry 2000; Fountas *et al.* 2006; Jiranyakul, Opiela 2010; Bhar, Mallik 2010; Conrad *et al.* 2010).

Our purpose in this paper is to investigate the relationship between the conditional means and conditional variance of inflation and output growth in Iran. Our main model for explaining the conditional means of the two series is a VAR (Vector Autoregressive) type GARCH-M (VAR-GARCH-M) model. We simultaneously estimate a time-varying variance-covariance matrix. As the conditional variance is just the variance of the one step ahead forecasting error, the GARCH model seems like a natural choice to study the effects of uncertainty. The multivariate GARCH-M approach has the advantage that one estimates the uncertainty measure and its effects together in a simultaneous model. The rest of the paper is structured as follows. Section 2 provides a brief theoretical background; section 3 outlines the econometric model; section 4 defines the data; section 5 presents and interprets the main results; and finally, section 6 concludes the paper.

### 2. Theoretical background

Economic theory can predict either a positive, negative or zero effect of inflation on output growth, depending on the specific assumptions of the model (Tobin 1965; Stockman 1981; Sidrauski 1967). Some papers (Gomme 1993; Jonees, Manuelli 1995) use endogenous growth models and find a negative growth effect of inflation. However, there is another theoretical link between inflation and economic growth. The wellknown hypothesis is from Friedman (1977) who argues that high inflation leads to more inflation uncertainty, and this uncertainty lowers economic efficiency and reduces output. Ball (1992), using a game theoretical framework, shows a formal derivation of Friedman's hypothesis that higher inflation causes more inflation uncertainty. Cukierman and Meltzer (1986), using Barro and Gordon (1983) model, predict that higher inflation uncertainty leads to more inflation. Holland (1995) argues that, in the presence of a stabilization motive on the policymaker, an increase in inflation uncertainty will invite a tight monetary policy response and a lower average inflation rate. Hence, Holland (1995) concludes that higher inflation uncertainty leads to less inflation rate. Dotsey and Sarte (2000), using a Cash-in-advance model, show that inflation variability has a positive effect on economic growth. They argue that risk averse agents will tend to save more during periods of uncertainty. This extra savings will then translate via higher investment into higher economic growth. Black (1987) describes that the choice of investing in a risky specialized technology will produce an economy with higher average growth. In other words, he argues that greater output growth uncertainty raises the average real growth rate. Deveraux (1989) extended Barro and Gordon (1983) model to show that output growth uncertainty can positively affect inflation.

The common feature of these apparently unrelated arguments is the systematic connection between inflation and economic growth and their respective uncertainties. To estimate these relationships simultaneously, we apply a BGARCH-in-Mean (BGARCH-M) model of output growth and inflation. In the applied BGARCH-M models, the dependent variables in the mean equations are inflation and output growth. The explanatory variables will contain variables that help to forecast growth and inflation in mean equations and their uncertainty measures in variance equations. Thus, the hypotheses that we are going to test with Iranian data are as follows:

- Is there a significant relationship between inflation and inflation uncertainty?
- Does inflation uncertainty reduce economic growth?
- Does economic growth uncertainty have any influence on the level of economic growth?
- Does economic growth uncertainty affect inflation?

#### 3. The model

Since Engle's (1982) paper, the ARCH model has become a popular methodology for assessing Friedman's hypothesis. Its popularity can be attributed to its ability to generate time varying measure of inflation and output uncertainty (Wilson 2006). The GARCH model of inflation and growth, which estimate the mean and variance equations jointly for each series, can be written as follows:

$$\pi_{t} = \mu_{1} + \sum_{i=1}^{m} \phi_{i} \pi_{t-i} + \sum_{i=1}^{m} \theta_{i} y_{t-i} + \varepsilon_{1, t}, \tag{1}$$

$$h_{1,t} = c_1 + a_1 \varepsilon_{1,t-1}^2 + b_1 h_{1,t-1}, \tag{2}$$

$$y_{t} = \mu_{2} + \sum_{i=1}^{m} \phi_{i} \pi_{t-i} + \sum_{i=1}^{m} \theta_{i} y_{t-i} + \varepsilon_{2,t},$$
(3)

$$h_{2,t} = c_2 + a_2 \varepsilon_{2,t-1}^2 + b_{21} h_{2,t-1}, \tag{4}$$

where  $\pi_t$ ,  $y_t$  denote the rate of inflation, and GDP growth, respectively. The residuals,  $\varepsilon_{1,t}$  and  $\varepsilon_{2,t}$ , are assumed to be normally distributed with a time varying conditional variances.  $h_{1,t}$  is the conditional variance of the residual term taken as inflation uncertainty at time t and  $h_{2,t}$  is the conditional variance of the residual term taken as growth uncertainty at time t. Equations (1) and (3) are the autoregressive representation of inflation and growth, and equations (2) and (4) are the GARCH (1, 1) representation of conditional variance (Heidari, Bashiri 2010, 2011).

The univariate volatility models have a limitation which is assumed that the conditional variance of each series is independent from all other series. This could be a significant limitation as there could be volatility spilovers between variables, which makes the univariate model misspecified. Moreover, the covariances between series also are of interest. The BGARCH models can potentially overcome these deficiencies of their univariate counterparts. In addition, there are many situations when empirical multivariate models of conditional heteroscedasticity can be used fruitfully (Brooks 2002).

BGARCH models are very similar to their univariate counterparts, except that the former also specify equations for how the covariance moves over time. Several different BGARCH formulations have been proposed in the literature, including the VECH, diagonal VECH and the BEKK approaches. This paper, however, employs BEKK approach. It is assumed that in each model, for simplicity, there are two variables, whose return variance and covariance are to be modelled.

To illustrate the BEKK approach, consider the following equation:

$$H_{t} = C_{0}^{/}C_{0} + A_{11}^{/}\varepsilon_{t-1}\varepsilon_{t-1}^{/}A_{11} + B_{11}^{/}H_{t-1}B_{11},$$

$$\varepsilon_{t} \mid \psi_{t-1} \approx N(0, H_{t}), \tag{5}$$

where  $H_t$  is a 2×2 conditional variance-covariance matrix that is always positive definite,  $\varepsilon_t$  is a 2×1 innovation (disturbance) vector,  $\psi_{t-1}$  represents the information set at time t-1, C is a diagonal 2×2 lower triangular matrix of parameters, A and B are 2×2 matrices. The model requires the estimation of 11 parameters (C has 3 elements, A and B each have 4 elements). In order to gain a better understanding of how the BEKK approach works, the elements are written out below:

$$H_{t} = \begin{bmatrix} h_{11t} & h_{12t} \\ h_{21t} & h_{22t} \end{bmatrix}, \ \varepsilon_{t} = \begin{bmatrix} u_{1t} \\ u_{2t} \end{bmatrix}, \ C = \begin{bmatrix} c_{11} & 0 \\ c_{21} & c_{22} \end{bmatrix}, \ A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, \ B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}.$$
 (6)

We see that this model economizes on parameters by imposing restrictions both across and within equations.

The diagonal BEKK model, takes A and B as diagonal matrices. For this case, the BEKK model is a restricted version of the VEC model with diagonal matrices (Franke et al. 2005).

The diagonal BEKK model is given by the following equations:

$$h_{11,t} = c_{11}^2 + a_{11}^2 \epsilon_{1,t-1}^2 + b_{11}^2 h_{11,t-1}, \tag{7}$$

$$h_{22,t} = c_{21}^2 + c_{22}^2 + a_{22}^2 \varepsilon_{2,t-1}^2 + b_{22}^2 h_{22,t-1}, \tag{8}$$

$$h_{12,t} = h_{21,t} = c_{11}c_{21} + b_{11}b_{22}h_{12,t-1} + a_{11}a_{22}\varepsilon_{1,t-1}^2\varepsilon_{2,t-1}^2.$$

$$\tag{9}$$

Under the assumption of conditional normality, the parameters of the BGARCH models of BEKK specifications can be estimated by maximizing the following log-likelihood function:

$$l(\theta) = -\frac{TN}{2}\log 2\pi - \frac{1}{2}\sum_{t=1}^{T}(\log\left|H_{t}\right| + \varepsilon_{t}'H_{t}^{-1}\varepsilon_{t}),\tag{10}$$

where  $\theta$  denotes all the unknown parameters to be estimated, N is the number of series in the system and T is the number of observations and other notations are defined before. The maximum likelihood estimate for  $\theta$  is asymptotically normal, and thus traditional procedures for statistical inference are applicable.

#### 4. Data

In our empirical analysis we use the Consumer Price Index (CPI) and the real Gross Domestic Product (GDP) at 1996 constant prices for Iran as proxies for the price level and output, respectively. The data have quarterly frequency and range from 1988:Q1 to 2008:Q4 as gathered from the Central Bank of Iran (2011). Inflation is measured by the difference of the log of CPI (Asteriou 2006):

$$\pi_t = (\ln \text{CPI}_t - \ln \text{CPI}_{t-1}) \times 400. \tag{11}$$

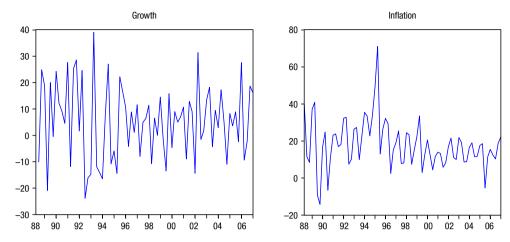


Fig. 1. Inflation and Growth Rate in the Iranian Economy

Real output growth (here after growth) is measured by the quarterly difference in the log of the GDP:

$$y_t = (\ln \text{GDP}_t - \ln \text{GDP}_{t-1}) \times 400.$$
 (12)

Figure 1 shows the inflation and growth rate in the Iranian economy during 1988–2008.

As Figure 1 shows the Iranian economy has experienced volatile inflation and growth rate during last three decades. The summary statistics for the data is given in Table 1. The large value of the Jargue-Bera statistic for inflation implies a deviation from normality. The value of the Jargue-Bera statistic for growth variable implies that, it is normally distributed.

Tabla 1	Lumma	ry Statistics	for	Iranian	Inflation	and Growth
Table 1	ı. Summa	iv Statistics	101	maman	IIIIIauon	anu Orowin

	Inflation	Growth
Mean	17.9419	5.26218
Median	16.7609	6.41796
Maximum	71.0550	39.0916
Minimum	-14.2872	-23.8725
Std. Dev.	13.0538	14.0937
Skewness	0.82163	0.07409
Kurtosis	5.84904	2.30495
Jargua-Bera	34.25522	1.57828
Probability	0.0000	0.454233

The Augmented Dickey-Fuller (ADF) and Phillips-Perron (PP)<sup>1</sup> Unit Root Tests are employed to test the integration level and the possible long-run relationship among the variables (Dickey, Fuller 1981; Phillips, Perron 1988). The PP procedures compute a residual variance, which is robust to auto-correlation, and are applied to test for unit roots as an alternative to the ADF unit root test (Katircioglu 2009).

To confirm the test results obtained from the ADF and PP tests, two more tests for unit roots have been employed in the present study, Firstly, *Kwiatkowski, Phillips, Schmidt, and Shin's* test (*KPSS*) (1992) is suggested to eliminate a possible low power against stationary near unit root processes which occurs in the *ADF* and PP tests. The KPSS test complements the ADF and PP tests in which the null hypothesis of KPSS test is that a series is stationary. This means that a stationary series is likely to have insignificant KPSS statistics and significant ADF and PP statistics.

The unit root test results reveal that both inflation and growth series are stationary at their levels<sup>2</sup>. As standard unit root tests, such as ADF, PP, and KPSS tests are biased towards the null of unit root in the presence of structural breaks on one hand, and visual inspection of the series in Figure 1 implies the existence of possible structural breaks on the other hand, we apply the endogenously determined multiple break tests introduced and applied by Bai and Perron (1998, 2003)<sup>3</sup>. Our results show that using most of these tests, we have no break in the mean of the series under consideration. However, we use Lee and Strazicich (2003) test to test the null hypothesis that the series under consideration has unit root against the alternative of stationary with two endogenous structural breaks<sup>4</sup>. The results reveal that in the presence of two possible structural breaks, the null of unit root for the series are rejected at 1 percent level of significance<sup>5</sup>.

#### 5. Estimates

We use a BGARCH model to simultaneously estimate the conditional means, variances, and covariances of inflation and growth. The first step to model a BGARCH model is specifying the mean equation by testing for serial dependence in the data under con-

<sup>&</sup>lt;sup>1</sup> As also mentioned by Katircioglu (2009), PP approach allows for the presence of unknown forms of autocorrelation with a structural break in the time series and conditional heteroscedasticity in the error term.

<sup>&</sup>lt;sup>2</sup> The results of unit root tests are available from the authors upon request.

<sup>&</sup>lt;sup>3</sup> A GAUSS algorithm to carry out these tests can be downloaded freely from Pierre Perron's home-page at http://econ.bu.edu/perron.

<sup>&</sup>lt;sup>4</sup> A GAUSS algorithm to carry out this test can be downloaded freely from Junsoo Lee's homepage at http://cba.ua.edu/~Jlee/gauss.

<sup>&</sup>lt;sup>5</sup> The results of Bai and Perron (1998, 2003) and Lee and Strazicich (2003) unit root test are available from the authors upon request.

sideration. Estimates of the mean equation for inflation rate and growth are based upon the following bivariate model:

$$\begin{bmatrix} \pi_t \\ y_t \end{bmatrix} = \begin{bmatrix} \mu_1 \\ \mu_2 \end{bmatrix} + \begin{bmatrix} \phi_1 & \phi_2 \\ \phi_3 & \phi_4 \end{bmatrix} \begin{bmatrix} \pi_{t-1} \\ y_{t-1} \end{bmatrix} + \begin{bmatrix} \theta_1 & \theta_2 \\ \theta_3 & \theta_4 \end{bmatrix} \begin{bmatrix} \pi_{t-2} \\ y_{t-2} \end{bmatrix} + \begin{bmatrix} \rho_1 & \rho_2 \\ \rho_3 & \rho_4 \end{bmatrix} \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \end{bmatrix} + \begin{bmatrix} v_t \\ \varepsilon_t \end{bmatrix}.$$
(13)

In order to test whether there are any remaining ARCH effects in the residuals, we use the LM test for ARCH in the residuals (see, e.g. Engle 1982). The results of the ARCH-LM test suggest that there is ARCH effect in the residuals. As higher order ARCH indicates persistence in the conditional variance, the model is estimated as a GARCH(1,1) process. The method for the estimation of parameters which we use is maximum log-likehood with BEKK approach<sup>6</sup>. As McAleer (2010) pointed out, between BEKK-GARCH model and its alternative approaches, the final choice should be based on model performance within the appropriate framework in which they are used. From a theoretical perspective, the optimal model for estimating conditional covariance and correlation is the BEKK model (McAleer 2010). Moreover, for the empirical work, the BEKK model is relatively simple in comparison to alternative models, which allows one to achieve reliable estimates of variance and covariances (Minovic 2009; Heidari, Molabahrami 2010). However, we used Constant Conditional Correlation (CCC) and Dynamic CC (DCC) models to estimate the model, and find best results with BEKK approach in terms of in-sample forecasting power. The estimated bivariate BEKK model is reported in Table  $2^7$ .

However, the coefficient of conditional variance of inflation in the mean equation is positive and insignificant, which means that inflation uncertainty does not affect the level of inflation. This result rejects Cukierman and Meltzer (1986), and Cukierman (1992) hypothesis that increases in inflation uncertainty raise the optimal inflation rate by increasing the incentive for the policy maker to create inflation surprises. In other words, our result suggests that inflation causes inflation uncertainty, supporting the Friedman–Ball hypothesis. This result is in line with Fountas (2001), Grier *et al.* (2004), Apergis (2004) and Berument *et al.* (2009).

Moreover, our empirical evidence shows that inflation uncertainty affects the level of economic growth inversely, supporting Friedman (1977) hypothesis. This is inline with Judson and Orphanides (1999), Wilson and Culver (1999), Hayford (2000), Wilson (2006), Hwang (2007) and Fang *et al.* (2009), where they find a negative relationship between inflation uncertainty and output growth for different countries.

Our empirical evidence also shows that growth uncertainty does not affect the level of economic growth, supporting Friedman (1968) hypothesis. Some recent studies including Fountas *et al.* (2004), Fountas and Karanasos (2006), Chatterjee and Shukayev (2006) and Fang *et al.* (2009) find no significant relationship between output growth

<sup>&</sup>lt;sup>6</sup> Heidari and Molabahrami (2010) explain why the BEKK approach is more convenient among the other specifications of BGARCH models.

<sup>&</sup>lt;sup>7</sup> An Eviews program to estimate this model is available from the authors upon request.

**Table 2.** Estimated parameters of bivariate BEKK model

	Coefficient	Std.Error	z–Statistic	Prob
$\mu_1$	14.68156	2.364256	6.209800	0.0000
φ <sub>1</sub>	0.128723	0.120038	1.072352	0.2836
φ <sub>2</sub>	20.041729	0.071510	0.583543	0.5595
$\theta_1$	-0.557626	0.086242	-6.465809	0.0000
$\theta_2$	0.143020	0.064076	2.232045	0.0256
$\rho_1$	0.023359	0.020650	1.131148	0.2580
$\rho_2$	0.023592	0.008845	2.667355	0.0076
$\mu_2$	10.32378	3.748091	2.754411	0.0059
φ <sub>3</sub>	-0.138493	0.131560	-1.052697	0.2925
$\phi_4$	-0.441259	0.157608	-2.799723	0.0051
$\theta_3$	-0.348366	0.185744	-1.875520	0.0607
$\theta_4$	-0.084866	0.145134	-0.584742	0.5587
$\rho_3$	-0.030085	0.0012879	2.335898	0.0195
$\rho_4$	0.007208	0.021703	0.332128	0.7398
c <sub>11</sub>	3.606652	1.491226	2.418582	0.0156
<i>b</i> <sub>11</sub>	-0.453760	0.220829	-2.054806	0.0399
<i>a</i> <sub>11</sub>	0.940544	0.244069	3.853593	0.0001
$c_{22}$	4.390737	4.367798	1.005252	0.3148
c <sub>21</sub>	-4.350780	4.153293	-1.047549	0.2948
b <sub>22</sub>	0.525242	0.286494	1.833345	0.0669
a <sub>22</sub>	0.762986	0.220164	3.465536	0.0005
	,			

and its uncertainty too. Finally, the empirical evidence shows that growth uncertainty affects the level of inflation. This result supports the Deveraux (1989) hypothesis, and is inline with Heidari and Bashiri (2011).

Equation (13) shows that these models allow for dynamic dependence between the volatility of the series under consideration. Figure 2 and 3 show the conditional covariance and variance of inflation and growth. It can be seen from the behavior of conditional covariance (Figure 2) that correlation between inflation and growth is unstable over time.

On the other hand, it has been frequently observed that volatility changes over time. We showed that inflation is more volatile than growth. In the model, estimated conditional variance of inflation has the greatest peak at the time.

Finally we checked the fitted model carefully. For diagnostic checking we used the Ljung-Box statistics of standardized residuals and those of its squared for inflation and growth.

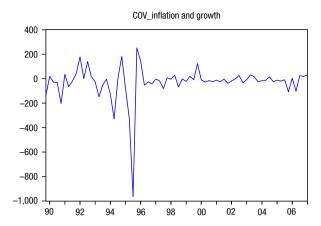


Fig. 2. Estimated conditional covariance for inflation and growth

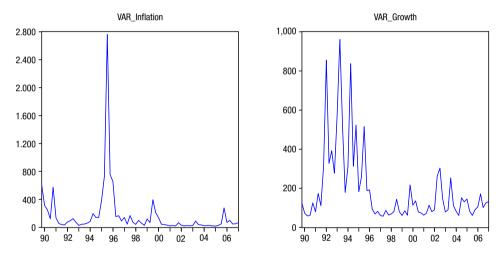


Fig. 3. Estimated conditional variances of inflation and growth

The Q-statistics for checking weather there are any ARCH effects left in the residuals show that autocorrelation is not significant in variance equations for inflation and growth. Thus, the check of the models shows is adequate for describing the conditional heteroscedasticity of the data.

#### 6. Conclusions

In this paper, we have investigated empirically the relationship between inflation, economic growth and their respective uncertainties in Iran. The study has used the period of 1988–2008 by using quarterly data and applying a VAR-type GARCH-M model. The method for the estimation of parameters which we use is maximum log-likelihood with BEKK approach. Our empirical results support a number of important conclusions:

(1) Inflation causes inflation uncertainty, supporting the Friedman-Ball hypothesis. This means that a change in inflation will lead to future expectations for inflation to be less certain in the case of Iran. (2) Inflation uncertainty affects the level of economic growth, supporting Friedman (1977) hypothesis. This also suggests that any uncertainty in future inflation rates will lead to uncertainties in future economic activity and growth rates. (3) Growth uncertainty does not affect the level of economic growth, supporting Friedman (1968) hypothesis. This means that actual economic growth rates are not statistically related to uncertainties about future growth rates. (4) And finally our empirical evidence shows that growth uncertainty affects the level of inflation, supporting Deveraux (1989) hypothesis. This important finding also suggests that uncertainties about the expected volume of economic activity and growth rate in Iran will have influence on inflation rates (leading to rises in inflation) in the economy. The present study has shown that since results are in line and some in contradiction with the other studies, research in searching the relationship between inflation, its uncertainty, and growth is still inconclusive in general and deserves further attention.

#### References

Apergis, N. 2004. Inflation, output growth, volatility and causality: evidence from panel data and the G7 countries, *Economics Letters* 83: 185–191. http://dx.doi.org/10.1016/j.econlet.2003.11.006

Asteriou, D. 2006. Applied econometrics: a modern approach using Eviews and Microfit. New York: Palgrave Macmillan.

Bai, J.; Perron, P. 1998. Estimating and testing linear models with multiple structural changes, *Econometrica* 66: 47–78. http://dx.doi.org/10.2307/2998540

Bai, J.; Perron, P. 2003. Computation and analysis of multiple structural change models, *Journal of Applied Econometrics* 18: 1–22. http://dx.doi.org/10.1002/jae.659

Ball, L. 1992. Why dose high inflation raise inflation uncertainty?, *Journal of Monetary Economics* 29: 371–388. http://dx.doi.org/10.1016/0304-3932(92)90032-W

Barro, R. J.; Gordon, D. B. 1983. Rules, discretion, and reputation in a model of monetary policy, *Journal of Monetary Economics* 12: 101–121. http://dx.doi.org/10.1016/0304-3932(83)90051-X

Berument, H.; Yalcin, Y.; Yildirim, J. 2009. The effect of inflation uncertainty on inflation: stochastic volatility in mean model within a dynamic framework, *Economic Modeling* 26: 1201–1207. http://dx.doi.org/10.1016/j.econmod.2009.05.007

Bhar, R.; Mallik, G. 2010. Inflation, inflation uncertainty and output growth in the USA, *Physica A* 389(23): 5503–5510. http://dx.doi.org/10.1016/j.physa.2010.06.063

Black, F. 1987. Business cycles and equilibrium, New York: Basil Blackwell.

Brooks, C. H. 2002. *Introductory econometrics for finance*. Cambridge: Cambridge University Press. Central Bank of the Islamic Republic of Iran. 2011. [online], [cited 25 September 2011]. Available from internet: http://www.cbi.ir/default\_en.aspx.

Chatterjee, P.; Shukayev, M. 2006. Are average growth rate and volatility related?, *Working Papers* 06-24, Bank of Canada.

Conrad, C.; Karanasos, M.; Zeng, N. 2010. The link between macroeconomic performance and variability in the UK, *Economic Letters* 106: 154–157. http://dx.doi.org/10.1016/j.econlet.2009.11.002

Cukierman, A.; Meltzer, A. 1986. A theory of ambiguity, credibility, and inflation under discretion and asymmetric information, *Econometrica* 54: 1099–1128. http://dx.doi.org/10.2307/1912324

Cukierman, A. 1992. Central bank strategy, credibility and independence. Cambridge: MIT Press.

Deveraux, M. 1989. A positive theory of inflation and inflation variance, *Economic Inquiry* 27: 105–116. http://dx.doi.org/10.1111/j.1465-7295.1989.tb01166.x

Dickey, D. A.; Fuller, W. A. 1981. Likelihood ratio statistics for autoregressive time series with a unit root, *Econometrica* 49: 1057–1072. http://dx.doi.org/10.2307/1912517

Dotsey, M.; Sarte, P. D. 2000. Inflation uncertainty and growth in a cash-in-advance economy, *Journal of Monetary Economics* 45: 631–655. http://dx.doi.org/10.1016/S0304-3932(00)00005-2

Engle, R. F. 1982. Autoregressive conditional heteroskedasticity with estimates of the variance of UK inflation, *Econometrica* 50: 987–1008. http://dx.doi.org/10.2307/1912773

Fang, W.; Miller, S.; Lee, C. 2009. Modeling the volatility of real GDP growth: the case of Japan revisited, *Japan and the World Economy* 21(3): 312–324. http://dx.doi.org/10.1016/j.japwor.2008.10.002

Fountas, S. 2001. The relationship between inflation and inflation uncertainty in the UK: 1885–1998, *Economics Letters* 74: 77–83. http://dx.doi.org/10.1016/S0165-1765(01)00522-5

Fountas, S.; Karanasos, M. 2006. The relationship between economic growth and real uncertainty in the G3, *Economic Modelling* 23: 638–647. http://dx.doi.org/10.1016/j.econmod.2006.03.002

Fountas, S.; Karanasos, M.; Mendoza, A. 2004. Output variability and economic growth: the Japanese case, *Bulletin of Economic Research* 56(4): 353–363. http://dx.doi.org/10.1111/j.1467-8586.2004.00209.x

Fountas, S.; Karanasos, M.; Kim, J. 2006. Inflation uncertainty, output growth uncertainty and macroeconomic performance, *Oxford Bulletin of Economics and Statistics* 68: 319–343. http://dx.doi.org/10.1111/j.1468-0084.2006.00164.x

Franke, J.; Hardle, W.; Hafer, Ch. 2005. *Introduction to Statistics of Financial Markets*. Available from Internet: http://www.quantlet.Com/mdstat/scripts/sfe/html/29.sfeframe 131.html.

Friedman, M. 1977. Inflation and unemployment, *Journal of Political Economy* 85: 451–472. http://dx.doi.org/10.1086/260579

Friedman, M. 1968. The role of monetary policy, American Economic Review 58: 1–17.

Gomme, P. 1993. Money and growth revisited: measuring the costs of in an endogenous growth model, *Journal of Monetary Economics* 32: 51–77. http://dx.doi.org/10.1016/0304-3932(93)90035-E

Grier, K.; Henry, O. T.; Olekalns, N.; Shields, K. 2004. The asymmetric effects of uncertainty on inflation and output growth, *Journal of Applied Econometrics* 19: 551–565. http://dx.doi.org/10.1002/jae.763

Grier, K.; Perry, M. J. 2000. The effects of real and nominal uncertainty on inflation and output growth: some GARCH-M evidence, *Journal of Applied Econometrics* 15: 45–58. http://dx.doi.org/10.1002/(SICI)1099-1255(200001/02)15:1<45::AID-JAE542>3.0.CO;2-K

Hayford, M. D. 2000. Inflation uncertainty, unemployment uncertainty and economic activity, *Journal of Macroeconomics* 22: 315–329. http://dx.doi.org/10.1016/S0164-0704(00)00134-8

Heidari, H.; Bashiri, S. 2010. Inflation and inflation uncertainty in Iran: an application of GARCH-in-Mean model with FIML method of estimation, *International Journal of Business and Development Studies* 2(1): 131–146.

Heidari, H.; Bashiri, S. 2011. An empirical reinvestigation of the effects of growth uncertainty on inflation in Iran: an application of GARCH-in-Mean models, *International Journal of Business and Development Studies* 3(1): 121–140.

Heidari, H.; Yengjeh, S. F. 2010. An empirical investigation of the effects of inflation uncertainty on economic growth in Iran, *EBES 2010*. Istanbul, Turkey.

Heidari, H.; Parvin, S.; Shakery, A.; Yengjeh, S. 2010. Impact of economic growth uncertainty on economic growth in Iran: some evidence from GARCH models, *Quarterly Iranian Economic Research* 43(2): 189–210.

Heidari, H.; Molabahrami, A. 2010. Portfolio optimization using multivariate GARCH models: evidence from Tehran stock market, *Journal of Finance Research* 30: 35–56.

Holland, S. A. 1993. Comment on inflation regimes and the sources of inflation uncertainty, *Journal of Money, Credit and Banking* 25: 514–520.

Holland, S. A. 1995. Inflation and uncertainty: tests for temporal ordering, *Journal of Money, Credit and Banking* 27: 827–837. http://dx.doi.org/10.2307/2077753

Hwang, Y. 2007. Causality between inflation and real growth, *Economic Letters* 94: 146–153. http://dx.doi.org/10.1016/j.econlet.2006.09.010

Jiranyakul, K.; Opiela, T. 2010. Inflation and inflation uncertainty in the ASEAN-economies, *Journal of Asian Economics* 21: 105–112. http://dx.doi.org/10.1016/j.asieco.2009.09.007

Jones, L.; Manuelli, R. 1995. Growth and the effects of inflation, *Journal of Economics Dynamics and Control* 19: 1405–1428. http://dx.doi.org/10.1016/0165-1889(94)00835-6

Judson, R.; Orphanides, A. 1999. Inflation, volatility and growth, *International Finance* 2: 117–138. http://dx.doi.org/10.1111/1468-2362.00021

Karanasos, M.; Kim, J. 2005. The inflation-output variability relationship in the G3: a bivariate GARCH (BEKK) approach, *Risk Letters* 1(2): 17–22.

Katircioglu, S. 2009. Revisiting the tourism-led growth hypothesis for Turkey using the bounds test and Johansen approach for cointegration, *Tourism Management* 30(1): 17–20. http://dx.doi.org/10.1016/j.tourman.2008.04.004

Komijani, A.; Nazari, R. 2009. Effect of government sizes on economic growth in Iran, *Quarterly Journal of the Economic Research* 9(3): 1–28.

Kwiatkowski, D.; Phillips, P. C. B.; Schmidt, P.; Shin, Y. 1992. Testing the null hypothesis of stationarity against the alternative of a unit root: how sure are we that economic time series have a unit root?, *Journal of Econometrics* 54(1–3): 159–178. http://dx.doi.org/10.1016/0304-4076(92)90104-Y

Lee, J.; Strazicich, M. C. 2003. Minimum LM unit root test with two structural breaks, *Review of Economics and Statistics* 63: 1082–1089. http://dx.doi.org/10.1162/003465303772815961

McAleer, M. 2010. Do we really need both BEKK and DCC? A tale of two multivariate GARCH models, *Discussion Paper* No. 738. Kyoto Institute of Economic Research, Kyoto University, Kyoto, Japan.

Minovic, J. Z. 2009. Modeling multivariate volatility processes: theory and evidence, *Theoretical and Applied Economics* 5(5): 21–44.

Mohammadi, T.; Akbari Fard, H. 2008. The effects of productivity shocks on economic growth in Iran, *Quarterly Iranian Economic Research* 10(35): 177–204.

Moshiri, S.; Jahangard, E. 2004. Information and communation technology and Iranian economic growth, *Quarterly Iranian Economic Research* 6(19): 55–78.

Narayan, P. K.; Narayan, S.; Smyth, R. 2009. Understanding the inflation-output nexus for China, *China Economic Review* 20: 82–90.

Phillips, P. C. B.; Perron, P. 1988. Testing for a unit root in time series regression, *Biometrica* 75: 335–346. http://dx.doi.org/10.1093/biomet/75.2.335

Shields, K.; Olekalns, N.; Henry, O. T.; Brooks, C. 2005. Measuring the response of macroeconomic uncertainty of shocks, *The Review of Economic and Statistics* 87(2): 362–370. http://dx.doi.org/10.1162/0034653053970276 Sidrauski, M. 1967. Inflation and economic growth, *Journal of Political Economy* 75: 796–810. http://dx.doi.org/10.1086/259360

Stockman, A. 1981. Anticipated inflation and the capital stock in a cash-in-advance economy, *Journal of Monetary Economics* 8: 387–393. http://dx.doi.org/10.1016/0304-3932(81)90018-0

Teresiene, D. 2009. Lithuanian stock market analysis using a set of GARCH models, *Journal of Business Economics and Management* 10(4): 349–360. http://dx.doi.org/10.3846/1611-1699.2009.10.349-360

Tobin, J. 1965. Money and economic growth, *Econometrica* 33: 671–684. http://dx.doi.org/10.2307/1910352

Wilson, B. 2006. The link between inflation, inflation uncertainty and output growth: new time series evidence from Japan, *Journal of Macroeconomics* 28: 609–620. http://dx.doi.org/10.1016/j.jmacro.2004.11.004

Wilson, B. K.; Culver, S.E. 1999. On measuring the response of real GDP growth to changes in inflation volatility, *Quarterly Journal of Business and Economics* 38: 3–15.

Hassan HEIDARI (PhD) is Dean of the Faculty of Economics and Management, Urmia University, Urmia, Iran. He earned his PhD from the University of New South Wales, Australia. His research interests include Applied Macroeconometrics, Macroeconomics Forecasting, Bayesian Econometrics, New-Keynesian Macroeconomics (Monetary Economics), and Time Series Analysis and Modelling. He has published in considerable amount of international peer review journals such as Romanian Journal of Economic Forecasting, Acta Oeconomica, Actual Problems of Economics, African Journal of Business Management, International Journal of Business and Development Studies, Financial Research, Quarterly Journal of Economic Research and Policies, Quarterly Journal of Quantitative Economics, Iranian Journal of Economic Research, Quarterly Journal of Research and Planning in Higher Education, Journal of Money and Economics, and Quarterly Iranian Economic Research.

Salih Turan KATIRCIOGLU (PhD) is Professor of Economics in the Department of Banking and Finance of Faculty of Business and Economics, Eastern Mediterranean University, Famagusta, North Cyprus, Via Mersin 10, Turkey. He graduated from the same institution and earned his PhD from Uludag University, Turkey. His research interests include applied time series econometrics, international trade, international finance, tourism economics, and economic growth issues. He serves as an editor in the *International Journal of Economic Perspectives*. He has previously published in considerable amount of international peer review journals such as Applied Economics, Tourism Management, Applied Economics Letters, The World Economy, Journal of Business Economics and Management, International Journal of Manpower, International Journal of Bank Marketing, and International Journal of Social Economics.

**Sahar BASHIRI** (MA) is a PhD Candidate, Department of Economics, University of Sistan and Baluchestan, Zahedan, Iran. She has already published papers in international peer review Journal of Business and Development Studies. Her research interests include Applied Macroeconometrics, and Time Series Modelling and Analysis.